

CURRICULUM VITAE

Jianchun Chu

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Personal Data

Date of birth: February 3, 1990 Sex: Male
Nationality: Chinese
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Research Interests

- Research areas: Differential Geometry, Partial Differential Equations.
- Some specific topics: Kähler geometry, Hermitian geometry, almost-Hermitian geometry, nonlinear elliptic and parabolic equations, complex Monge-Ampère equations.

Employment

- Assistant Professor, Peking University, 2021-present.
- Boas Assistant Professor, Northwestern University, 2018-2021.
Advisor: Valentino Tosatti and Ben Weinkove
- Postdoc, Chinese Academy of Sciences, 2017-2019 (*on leave 2018-2019*).
Advisor: Liqun Zhang

Education

- Ph.D. in Mathematics, Peking University, 2012-2017.
Advisor: Gang Tian
(Visiting Student, Northwestern University, September 2015 – September 2016.
Advisor: Aaron Naber)
- B.S. in Mathematics and Applied Mathematics, Beijing Institute of Technology, 2008-2012.

Honors and Awards

- Outstanding Graduate (Beijing, China), 2017.
- National Scholarship for Graduate Student (China), 2016.

- National Scholarship for Graduate Student (China), 2015.
- National Scholarship for Graduate Student (China), 2013.
- Outstanding Graduate (Beijing, China), 2012.
- National Scholarship (China), 2010.
- National Scholarship (China), 2009.

Grants

- Participant (PI: Bin Zhou), National Natural Science Foundation of China (No. 12271008), *Regularity of complex Monge-Ampère equation and geometric inequalities*, 2023–2026.
- PI, The Fundamental Research Funds for the Central Universities, Peking University, *Partial differential equations in geometry*, 2021–2024.

Publications and Preprints

1. (With M.-C. Lee and J. Zhu) *Singular positive mass theorem with arbitrary ends*, preprint, arXiv: 2210.08261.
2. (With M.-C. Lee and K.-K. Kwong) *Rigidity on non-negative intermediate curvature*, preprint, arXiv: 2208.12240.
3. (With M.-C. Lee) *Hypercritical deformed Hermitian-Yang-Mills equation revisited*, to appear in *J. Reine Angew. Math.*
4. (With M.-C. Lee) *Ricci-DeTurck flow from rough metrics and applications*, preprint, arXiv: 2204.05843.
5. (With N. McCleerey) *Lelong Numbers of m -Subharmonic Functions Along Submanifolds*, preprint, arXiv: 2204.01963.
6. (With P.-Y. Chan, M.-C. Lee and T.-Y. Tsang) *Monotonicity of the p -Green functions*, preprint, arXiv: 2202.13832.
7. (With M.-C. Lee) *Kähler tori with almost non-negative scalar curvature*, to appear in *Commun. Contemp. Math.*
8. (With L. Huang and J. Zhang) *Fully non-linear elliptic equations on compact almost Hermitian manifolds*, *Calc. Var. Partial Differential Equations* **62** (2023), no. 3, Paper No. 105, 34 pp.
9. (With M.-C. Lee) *Hypercritical deformed Hermitian-Yang-Mills equation*, preprint, arXiv: 2107.13192.

10. (With M.-C. Lee and R. Takahashi) *A Nakai-Moishezon type criterion for supercritical deformed Hermitian-Yang-Mills equation*, to appear in *J. Differential Geom.*
11. (With M.-C. Lee) *On the Hölder estimate of Kähler-Ricci flow*, to appear in *Int. Math. Res. Not. IMRN*.
12. (With M.-C. Lee) *Conformal tori with almost non-negative scalar curvature*, *Calc. Var. Partial Differential Equations* **61** (2022), no. 3, Paper No. 114, 20 pp.
13. (With N. McCleerey) *Fully non-linear degenerate elliptic equations in complex geometry*, *J. Funct. Anal.* **281** (2021), no. 9, Paper No. 109176, 45 pp.
14. (With M.-C. Lee and L.-F. Tam) *Kähler manifolds with negative k -Ricci curvature*, *Trans. Amer. Math. Soc.* **375** (2022), no. 11, 7925–7944.
15. (With H. Jiao) *Curvature estimates for a class of Hessian type equations*, *Calc. Var. Partial Differential Equations* **60** (2021), no. 3, 90.
16. *A simple proof of curvature estimate for convex solution of k -Hessian equation*, *Proc. Amer. Math. Soc.* **149** (2021), no. 8, 3541–3552.
17. (With T. C. Collins and M.-C. Lee) *The space of almost calibrated $(1, 1)$ forms on a compact Kähler manifold*, *Geom. Topol.* **25** (2021), no. 5, 2573–2619.
18. (With N. McCleerey) *$C^{1,1}$ regularity of geodesics of singular Kähler metrics*, *J. Lond. Math. Soc. (2)* **104** (2021), no. 1, 66–96.
19. *$C^{1,1}$ regularity of degenerate complex Monge-Ampère equations and some applications*, *Anal. PDE* **14** (2021), no. 6, 1671–1700.
20. *$C^{1,1}$ regularity of geodesics in the space of volume forms*, *Calc. Var. Partial Differential Equations* **58** (2019), no. 6, Art. 194, 7 pp.
21. (With L. Huang and X. Zhu) *The Fu-Yau equation on compact astheno-Kähler manifolds*, *Adv. Math.* **346** (2019), 908–945.
22. (With L. Huang and X. Zhu) *The Fu-Yau equation in higher dimensions*, *Peking Math. J.* **2** (2019), no. 1, 71–97.
23. (With L. Huang and X. Zhu) *The 2-nd Hessian type equation on almost Hermitian manifolds*, preprint, arXiv: 1707.04072.
24. (With V. Tosatti and B. Weinkove) *$C^{1,1}$ regularity for degenerate complex Monge-Ampère equations and geodesic rays*, *Comm. Partial Differential Equations* **43** (2018), no. 2, 292–312.
25. (With B. Zhou) *Optimal regularity of plurisubharmonic envelopes on compact Hermitian manifolds*, *Sci. China Math.* **62** (2019), no. 2, 371–380.

26. (With V. Tosatti and B. Weinkove) *On the $C^{1,1}$ regularity of geodesics in the space of Kähler metrics*, Ann. PDE **3** (2017), no. 2, Art. 15, 12 pp.
27. *Quantitative stratification of F -subharmonic functions*, Comm. Anal. Geom. **29** (2021), no. 6, 1335–1389.
28. *The parabolic Monge-Ampère equation on compact almost Hermitian manifolds*, J. Reine Angew. Math. **761** (2020), 1–24.
29. (With V. Tosatti and B. Weinkove) *The Monge-Ampère equation for non-integrable almost complex structures*, J. Eur. Math. Soc. (JEMS) **21** (2019), no. 7, 1949–1984.
30. *$C^{2,\alpha}$ regularities and estimates for nonlinear elliptic and parabolic equations in geometry*, Calc. Var. Partial Differential Equations **55** (2016), no. 1, Art. 8, 20 pp.
31. *The complex Monge-Ampère equation on some compact Hermitian manifolds*, Pacific J. Math. **276** (2015), no. 2, 369–386.

Invited Talks

1. Geometric Analysis Seminar, School of Mathematical Sciences, Xiamen University, China, March 21st, 2023.
Title: Fully non-linear elliptic equations in almost Hermitian geometry (Online)
2. Seminar, School of Mathematics and Statistics, Beijing Institute of Technology, China, December 14th, 2022.
Title: Kähler tori with almost non-negative scalar curvature (Online)
3. Forum on Complex Geometry for Youth 2022, Chern Institute of Mathematics, Nankai University, China, December 3rd–5th, 2022.
Title: A Nakai-Moishezon type criterion for supercritical deformed Hermitian-Yang-Mills equation (Online, December 3rd, 2022)
4. Shanghai Maths Seminar 2022 (Communication in Analytic and Complex Geometry) (ShanghaiTech University, University of Chinese Academy of Sciences, University of Science and Technology of China, Tongji University), School of Mathematical Sciences, Tongji University, China, December 2nd, 2022.
Title: Fully non-linear elliptic equations on compact almost Hermitian manifolds (Online)
5. Workshop on Geometric Analysis in Hangzhou 2022, School of Mathematical Sciences, Zhejiang University, China, November 23th–24th, 2022.
Title: k -Ricci curvature in Kähler geometry (Online, November 24th, 2022)
6. Seminar, School of Mathematics, Hunan University, China, November 10th, 2022.
Title: A Nakai-Moishezon type criterion for supercritical deformed Hermitian-Yang-Mills equation (Online)
7. Complex Analysis and Elliptic PDE's Seminar, Faculty of Mathematics and Computer Science, Jagiellonian University, Poland, October 24th, 2022.

Title: Fully non-linear elliptic equations on compact almost Hermitian manifolds (Online)

8. Geometric Analysis Seminar, Institute for Theoretical Sciences, Westlake University, China, October 12th, 2022.
Title: The solvability of hypercritical deformed Hermitian-Yang-Mills equation (Online)
9. Seminar, Institute of Mathematics, Academy of Mathematics and Systems Science, Chinese Academy of Sciences, China, September 26th, 2022.
Title: A Nakai-Moishezon type criterion for supercritical deformed Hermitian-Yang-Mills equation (Online)
10. Workshop on Geometric Analysis 2022, Research Center for Mathematics and Interdisciplinary Sciences, Shandong University, China, September 5th–9th, 2022.
Title: A Nakai-Moishezon type criterion for supercritical deformed Hermitian-Yang-Mills equation (Online, September 5th, 2022)
11. 2022 International Conference on PDEs and Geometric Analysis, School of Mathematical Sciences, Shanghai Jiao Tong University, China, June 20th–24th, 2022.
Title: Hypercritical deformed Hermitian-Yang-Mills equation (Online, June 23th, 2022)
12. Workshop on Nonlinear Elliptic Equation and Geometric Analysis, School of Mathematics and Institute for Advanced Study in Mathematics, Harbin Institute of Technology, China, June 3rd–5th, 2022.
Title: k -Ricci curvature in Kähler geometry (Online, June 3rd, 2022)
13. Differential Geometry Seminar, Department of Mathematics, Zhejiang Normal University, China, May 17th, 2022.
Title: k -Ricci curvature and positivity of canonical bundle (Online)
14. Seminar, Faculty of Mathematics and Statistics, Hubei University, China, March 29th, 2022.
Title: Kähler tori with almost non-negative scalar curvature (Online)
15. Convergence or Scalar Curvature Seminar (Organized by Brian Allen, Edward Bryden, and Demetre Kazaras), USA, March 25th, 2022.
Title: Kähler tori with almost non-negative scalar curvature (Online)
16. Differential Geometry Seminar, School of Mathematics and Systems Science, Beihang University, China, March 4th, 2022.
Title: Kähler tori with almost non-negative scalar curvature (Online)
17. Complex Analysis, Harmonic Analysis, and Complex Geometry seminar, Department of Mathematics, Rutgers University - New Brunswick, USA, January 21st, 2022.
Title: On k -Ricci curvature for Kähler manifolds (Online)
18. Workshop on Complex Geometry, Beijing International Center for Mathematical Research, Peking University, China, January 11th, 2022.
Title: Hypercritical deformed Hermitian-Yang-Mills equation

19. Seminar, School of Mathematical Sciences, University of Electronic Science and Technology of China, China, December 3rd, 2021.
Title: k -Ricci curvature in Kähler geometry (Online)
20. Seminar, School of Mathematical Sciences, Peking University, China, November 11th, 2021.
Title: Degenerate complex Hessian equation on compact Kähler manifolds
21. Seminar, School of Mathematical Sciences, Shanghai Jiao Tong University, China, November 10th, 2021.
Title: k -Ricci curvature and positivity of canonical bundle (Online)
22. Beijing-Saint Petersburg Mathematics Colloquium (Online), School of Mathematical Sciences, Peking University, China, November 04, 2021.
Title: Kähler manifolds with quasi-negative k -Ricci curvature (Online)
23. Seminar, Institute of Mathematics, Academy of Mathematics and Systems Science, Chinese Academy of Sciences, China, November 2nd, 2021.
Title: The solvability of hypercritical deformed Hermitian-Yang-Mills equation
24. Seminar, Institute of Mathematics, Academy of Mathematics and Systems Science, Chinese Academy of Sciences, China, October 27th, 2021.
Title: On the Hölder estimate of Kähler-Ricci flow
25. Workshop on Geometric Analysis 2021, School of Statistics and Mathematics, Yunnan University of Finance and Economics, China, May 24th–28th, 2021.
Title: On the Hölder estimate of Kähler-Ricci flow (Online, May 28th, 2021)
26. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, April 29, 2021.
Title: $C^{1,1}$ estimate for degenerate complex Hessian equation (Online)
27. Geometric Analysis Seminar, Department of Mathematics and Statistics, McGill University, Canada, March 24th, 2021.
Title: The k -Ricci curvature in Kähler geometry (Online)
28. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, February 4th, 2021.
Title: The k -Ricci curvature in complex geometry (Online)
29. Seminar, School of Mathematics and Statistics, Beijing Institute of Technology, China, December 29th, 2020.
Title: Some fully non-linear PDEs in complex geometry (Online)
30. PDE Seminar, Institute of Mathematics, Academy of Mathematics and Systems Science, Chinese Academy of Sciences, China, December 4th, 2020.
Title: Fully non-linear PDEs and geometric applications (Online)

31. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, September 24th, 2020.
Title: The deformed Hermitian-Yang-Mills equation and the space of almost calibrated $(1, 1)$ forms (Online)
32. Geometric Analysis Seminar, Beijing International Center for Mathematical Research, Peking University, China, April 29th, 2020.
Title: The space of almost calibrated $(1, 1)$ forms on a compact Kähler manifold (Online)
33. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, April 9th, 2020.
Title: A priori estimate for the complex Monge-Ampère equation (Online)
34. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, January 9th, 2020.
Title: A Liouville Theorem for the complex Monge-Ampère equation
35. Geometric Analysis Seminar, School of Mathematical Sciences, Peking University, China, September 6th, 2019.
Title: $C^{1,1}$ regularity of geodesics of singular Kähler metrics
36. Geometric Analysis Seminar, School of Mathematics and Systems Science, Beihang University, China, September 5th, 2019.
Title: Complex Monge-Ampère equation and its geometric applications
37. Geometric Analysis Seminar, School of Mathematical Sciences, Zhejiang University, China, August 26th, 2019.
Title: Complex Monge-Ampère equation
38. Geometric Analysis workshop – Some topics in differential geometry, School of Mathematical Sciences, Peking University, China, July 10th, 2019.
Title: $C^{1,1}$ regularity of geodesics of singular Kähler metrics
39. International Conference on Partial Differential Equations and Applications, In Honor of 75th Birthday of Professor Haïm Brezis, School of Mathematical Sciences, Beijing Normal University, China, July 1st-3rd, 2019.
Title: $C^{1,1}$ regularity of geodesics of singular Kähler metrics (July 2nd, 2019)
40. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, April 4th, 2019.
Title: Stability of solutions of complex Monge-Ampère equations
41. AMS Sectional Meeting (Spring Central and Western Joint Sectional Meeting), Special Session on Analysis of Nonlinear Geometric Equations, Department of Mathematics, University of Hawai'i at Mañoa, USA, March 22nd–24th, 2019.
Title: $C^{1,1}$ regularity of geodesics of singular Kähler metrics (March 24th, 2019)
42. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, October 11th, 2018.

Title: Geometric estimates for complex Monge-Ampère equations

43. Geometric Analysis Seminar, School of Mathematical Sciences, Zhejiang University, China, April 2nd, 2018.
Title: The local $C^{1,1}$ regularity of quasi-psh envelopes in nef and big classes
44. Workshop on Geometric Analysis 2018 (Peking University, University of Science and Technology of China, Zhejiang University), School of Mathematical Sciences, Zhejiang University, China, March 31st–April 1st, 2018.
Title: The Fu-Yau equation on compact astheno-Kähler manifolds (March 31st, 2018)
45. Differential geometry and geometric analysis seminar, Department of Mathematics, Nanjing University, China, March 17th, 2018.
Title: Degenerate complex Monge-Ampère equation and its geometric applications
46. Workshop in complex geometry, Department of Mathematics, Southern University of Science and Technology, China, December 3rd, 2017.
Title: The Fu-Yau equation with negative slope parameter
47. Complex analysis Seminar, Institute of Mathematics, Academy of Mathematics and Systems Science, Chinese Academy of Sciences, China, November 21st, 2017.
Title: Optimal regularity of Plurisubharmonic envelopes on compact Hermitian manifolds
48. Geometric Analysis Seminar, School of Mathematical Sciences, Peking University, China, November 1st, 2017.
Title: Second order estimate for general complex Monge-Ampère equations
49. Chinese Mathematical Society 2017 Annual Conference, Special Session on Geometry and Topology, School of Mathematics and Computational Science, Xiangtan University, China, October 20th–24th, 2017.
Title: The $C^{1,1}$ regularity of geodesics in the space of Kähler metrics (October 21st, 2017)
50. Workshop on Geometric Analysis for Youth 2017, School of Mathematical Sciences, Zhejiang University, China, July 4th–5th, 2017.
Title: The $C^{1,1}$ regularity of geodesics in the space of Kähler metrics (July 4th, 2017)
51. Workshop on Geometric Analysis, School of Mathematical Sciences, Capital Normal University, China, May 22nd–26th, 2017.
Title: The Monge-Ampère equation on compact almost Hermitian manifolds (May 22nd, 2017)
52. Colloquium, School of Mathematical Sciences, Beijing Normal University, China, December 18th, 2016.
Title: The Monge-Ampère equation for non-integrable almost complex structures
53. Geometric Analysis Seminar, School of Mathematical Sciences, Peking University, China, September 30th, 2016.
Title: The Monge-Ampère equation for non-integrable almost complex structures

54. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, April 14th, 2016.
Title: Complex Monge-Ampère equations with right hand side in L^p
55. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, February 26th, 2016.
Title: Regularity of psh envelopes
56. Informal Geometric Analysis Seminar, Department of Mathematics, Northwestern University, USA, October 1st, 2015.
Title: $C^{2,\alpha}$ estimates for some nonlinear elliptic equations of second order in geometry
57. Workshop on Geometric Analysis, School of Mathematical Sciences, Xiamen University, China, May 17th–21st, 2015.
Title: $C^{2,\alpha}$ estimates for some nonlinear elliptic equations in complex geometry (May 19th, 2015)
58. Mini-conference in Complex Geometry, Department of Mathematics, Nanjing University, China, April 10th–11th, 2015.
Title: Soliton-type metrics and Kähler-Ricci flow on symplectic quotients (April 10th, 2015)
59. Autumn Workshop on Complex Geometry and Singularity Theory, Department of Mathematics, Nanjing University, China, November 1st–2nd, 2014.
Title: $C^{2,\alpha}$ estimates for nonlinear elliptic equations of second order in geometry (November 1st, 2014)
60. Geometric Analysis Seminar, Beijing International Center for Mathematical Research, Peking University, China, October 21st, 2014.
Title: $C^{2,\alpha}$ estimates for some nonlinear elliptic equations of second order in geometry

Mini-courses and Lecture series

1. 2022 Summer Short Course, Chern Institute of Mathematics, Nankai University, China, July 18th-August 11th, 2022.
Introduction to partial differential equations (July 18th, 20th, 22th, 26th, 28th, August 1st, 3rd, 5th, 9th, 11th, 2022).
2. 2020 Summer School on Differential Geometry, Beijing International Center for Mathematical Research, Peking University, China, August 3rd-14th, 2020.
Introduction to partial differential equations (August 3rd, 4th, 5th, 6th, 7th, 10th, 11th, 12th, 13th, 14th, 2020).
3. Lecture Series, Center for Applied Mathematics, Tianjin University, China, August 6th-8th, 2019.
Complex Monge-Ampère equation and its geometric applications (August 6th, 7th, 8th, 2019).

Teaching and TA Experiences

Courses Taught at Peking University:

- Advanced Mathematics (B) (1), Fall, 2022.
- Advanced Mathematics (B) (2), Spring, 2022.

Courses Taught at Northwestern University:

- Math 228-1, Multivariable Differential Calculus for Engineering, Winter, 2021.
- Math 228-1, Multivariable Differential Calculus for Engineering, Fall, 2020.
- Math 228-1, Multivariable Differential Calculus for Engineering, Winter, 2020.
- Math 228-1, Multivariable Differential Calculus for Engineering, Fall, 2019.
- Math 230-0, Differential Calculus of Multivariable Functions, Spring, 2019.
- Math 220-0, Differential Calculus of One Variable Functions, Fall, 2018.

Teaching Assistant at University of Chinese Academy of Sciences:

- Calculus, Spring, 2018.
- Calculus, Fall, 2017.

Teaching Assistant at Peking University:

- Calculus, Fall, 2016.
- Differentiable Manifolds, Spring, 2015.
- Calculus, Fall, 2014.
- Differentiable Manifolds, Spring, 2014.
- Differentiable Manifolds, Spring, 2013.

Professional Services

- Referee for: Acta Mathematica Sinica (English Series), Advances in Mathematics, Analysis & PDE, Calculus of Variations and Partial Differential Equations, Communications in Partial Differential Equations, Communications on Pure and Applied Mathematics, Complex Manifolds, Frontiers of Mathematics in China, International Mathematics Research Notices, Journal of Functional Analysis, Journal of Geometric Analysis, Journal of the European Mathematical Society, Mathematische Nachrichten, Mathematische Zeitschrift, Methods and Applications of Analysis, Peking Mathematical Journal, Proceedings of the American Mathematical Society, Pure and Applied Mathematics Quarterly, Revista Matemática Iberoamericana, Taiwanese Journal of Mathematics.